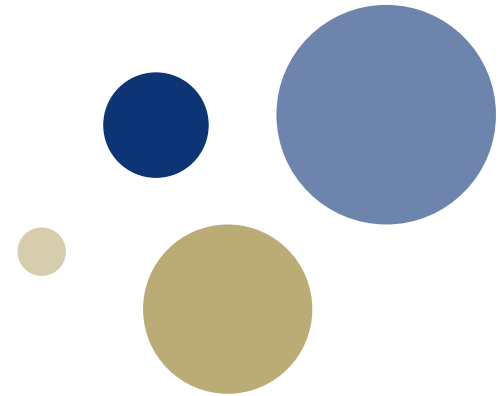




**NTNU – Trondheim**  
Norwegian University of  
Science and Technology



# **Nanothermodynamics to bridge nano and mesoscopic scales**

Sondre K. Schnell

Department of Materials Science and Engineering

Faculty of Natural Science

NTNU

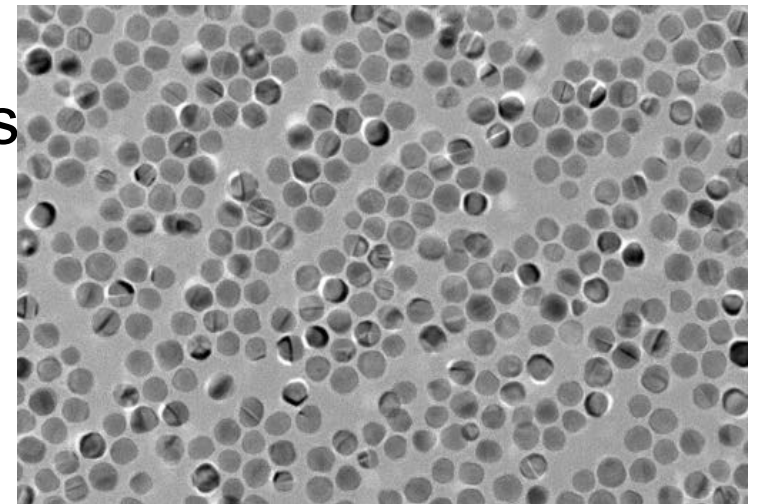
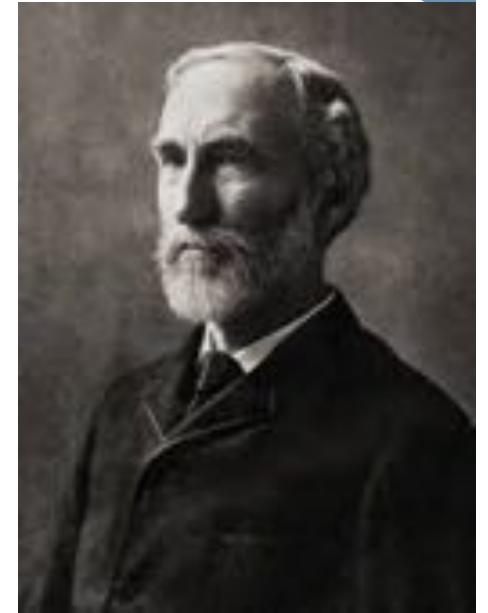
# Outline



- Thermodynamics and small systems
- Small system method
- Sampling from MD trajectories
- What to calculate
- Systems of interest

# Thermodynamics

- Thermodynamics is for "large" systems
  - $10^{23}$  atoms ++
- Smaller and smaller systems
- Thermodynamics for "small" systems

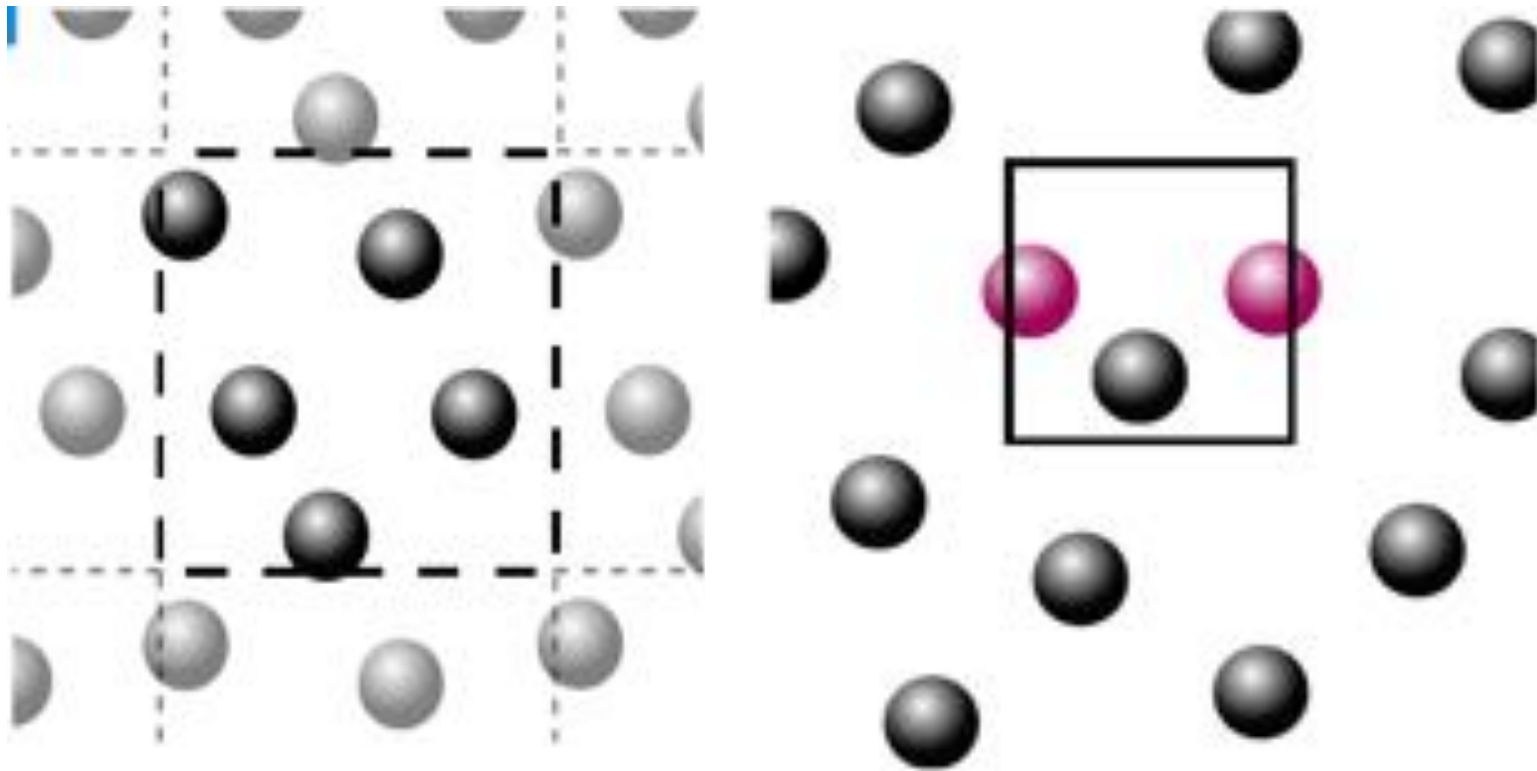


# Hill's thermodynamics



- "Nanothermodynamics" or "thermodynamics of small systems"
- $dU_t = TdS_t - pdV + \mu dV_t + \varepsilon dN$
- Divides the system in  $N$  clusters
- $\varepsilon$  is a sub-division potential
- "Correction" due to small size

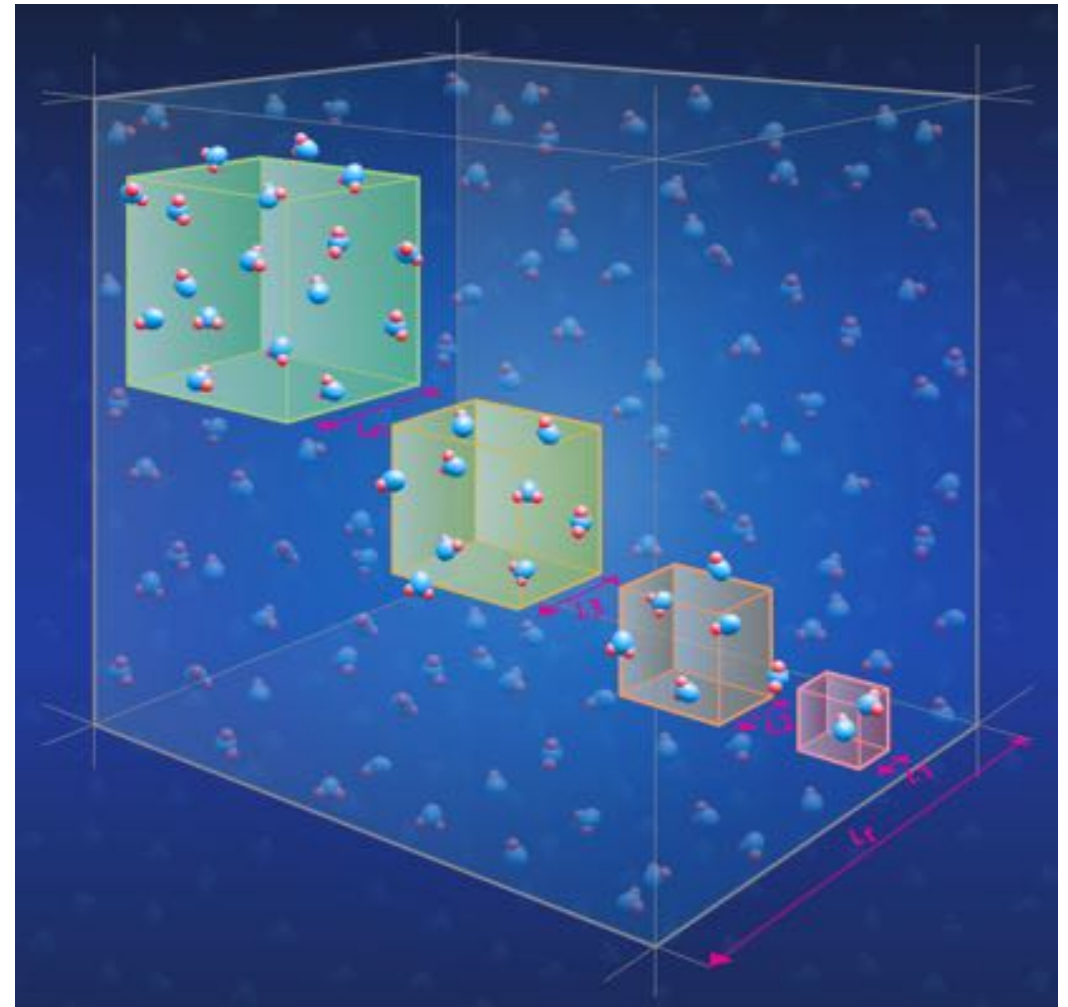
# Small system method



- Creating a small "cut-out" from a system makes it deviate from a periodic system

# Scaling

- Scaling
- Systematically changing the size
- Properties from the small systems calculated for each size

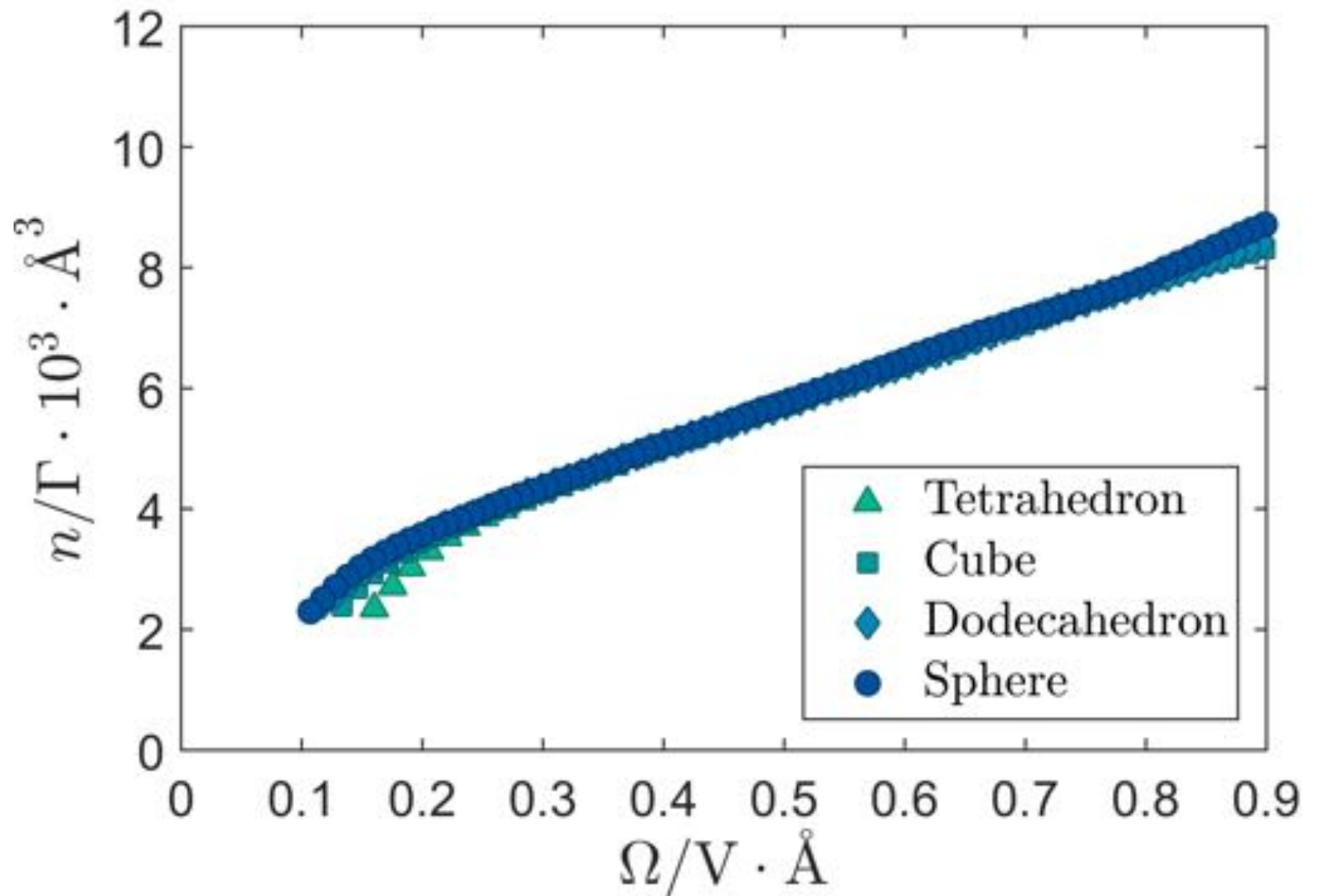
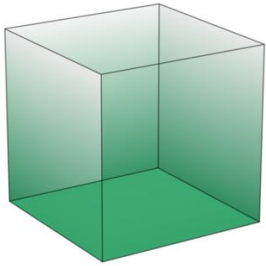
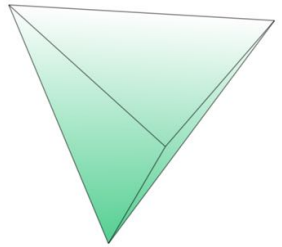


# Fluctuations



- $\frac{1}{\Gamma} = k_B T \left( \frac{\partial \ln \bar{N}}{\partial \mu} \right)_{T,V} = \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}$
- $\left( \frac{\partial \hat{H}}{\partial \bar{N}_i} \right)_{T,V,\mu} = \frac{\overline{UN_i} - \overline{U} \overline{N_i} + \overline{N_i} k_B T}{\overline{N_i^2} - \overline{N_i}^2}$
- $G_{\alpha\beta} = V \frac{\langle N_\alpha N_\beta \rangle - \langle N_\alpha \rangle \langle N_\beta \rangle}{\langle N_\alpha \rangle \langle N_\beta \rangle} - \frac{\delta_{\alpha\beta}}{c_\alpha} =$   
 $4\pi \int_0^\infty \left[ g_{\alpha\beta}^{\mu VT}(r) - 1 \right] r^2 dr \approx$   
 $4\pi \int_0^R \left[ g_{\alpha\beta}^{NVT}(r) - 1 \right] r^2 dr$

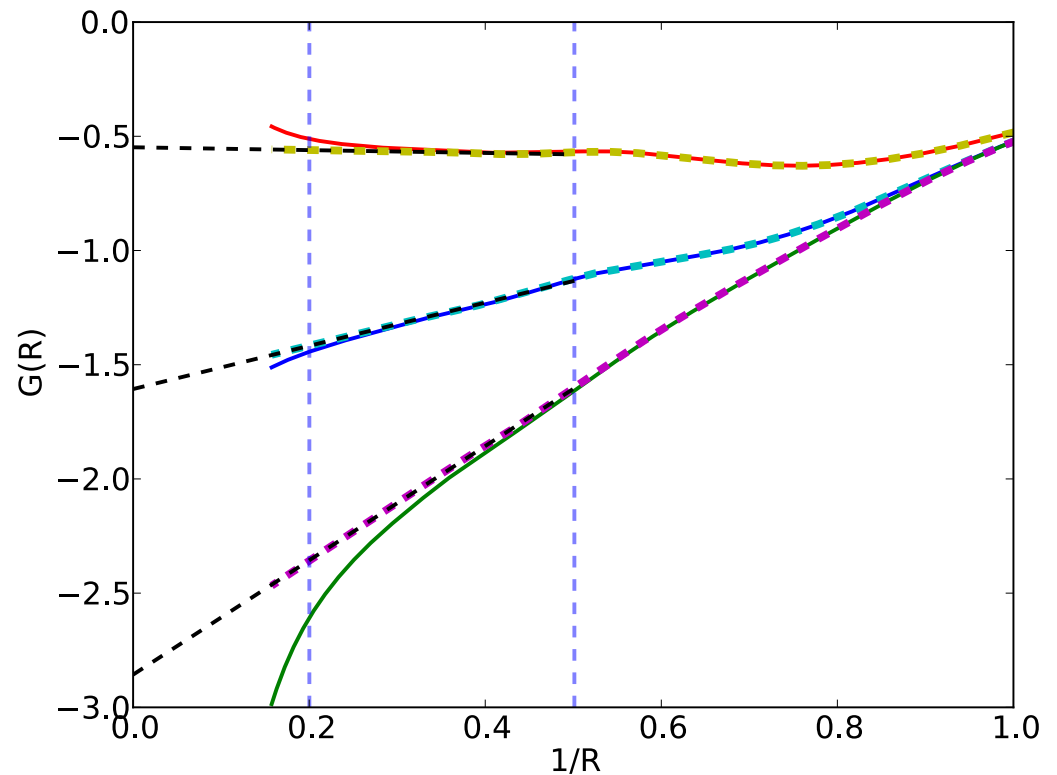
# Thermodynamic factors

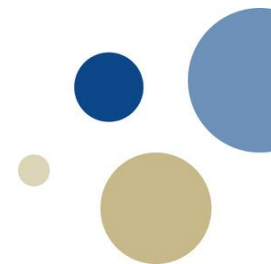




# Kirkwood-Buff theory

$$G_{\alpha\beta}^V \equiv \frac{1}{V} \int_V \int_V (g_{\alpha\beta}(r_{12}) - 1) d\mathbf{r}_1 d\mathbf{r}_2$$
$$= 4\pi \int_0^{2R} (g_{\alpha\beta}(r) - 1) r^2 \left(1 - \frac{3r}{4R} + \frac{r^3}{16R^3}\right) dr \equiv G_{\alpha\beta}(R)$$

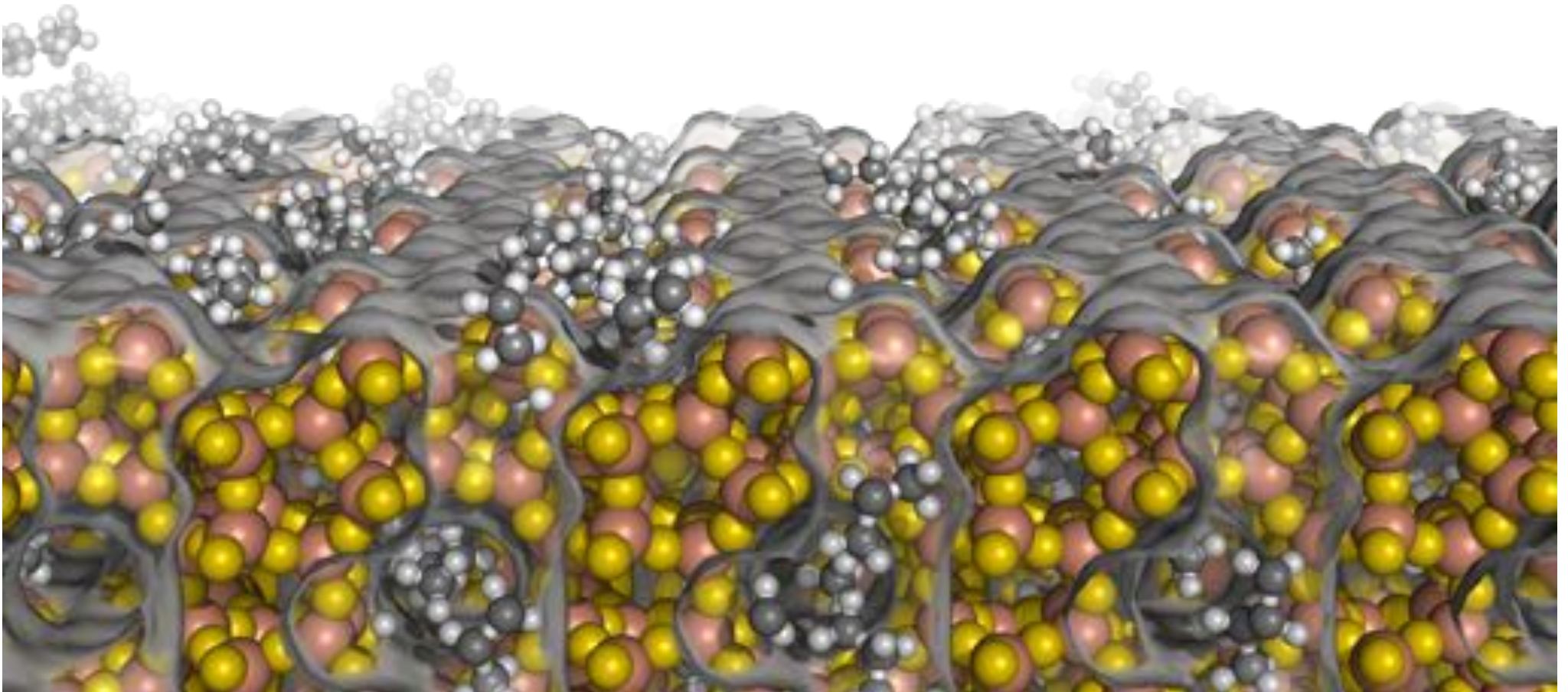




# **FUTURE WORK**

# Surface properties

- Surfaces are thin → Small systems



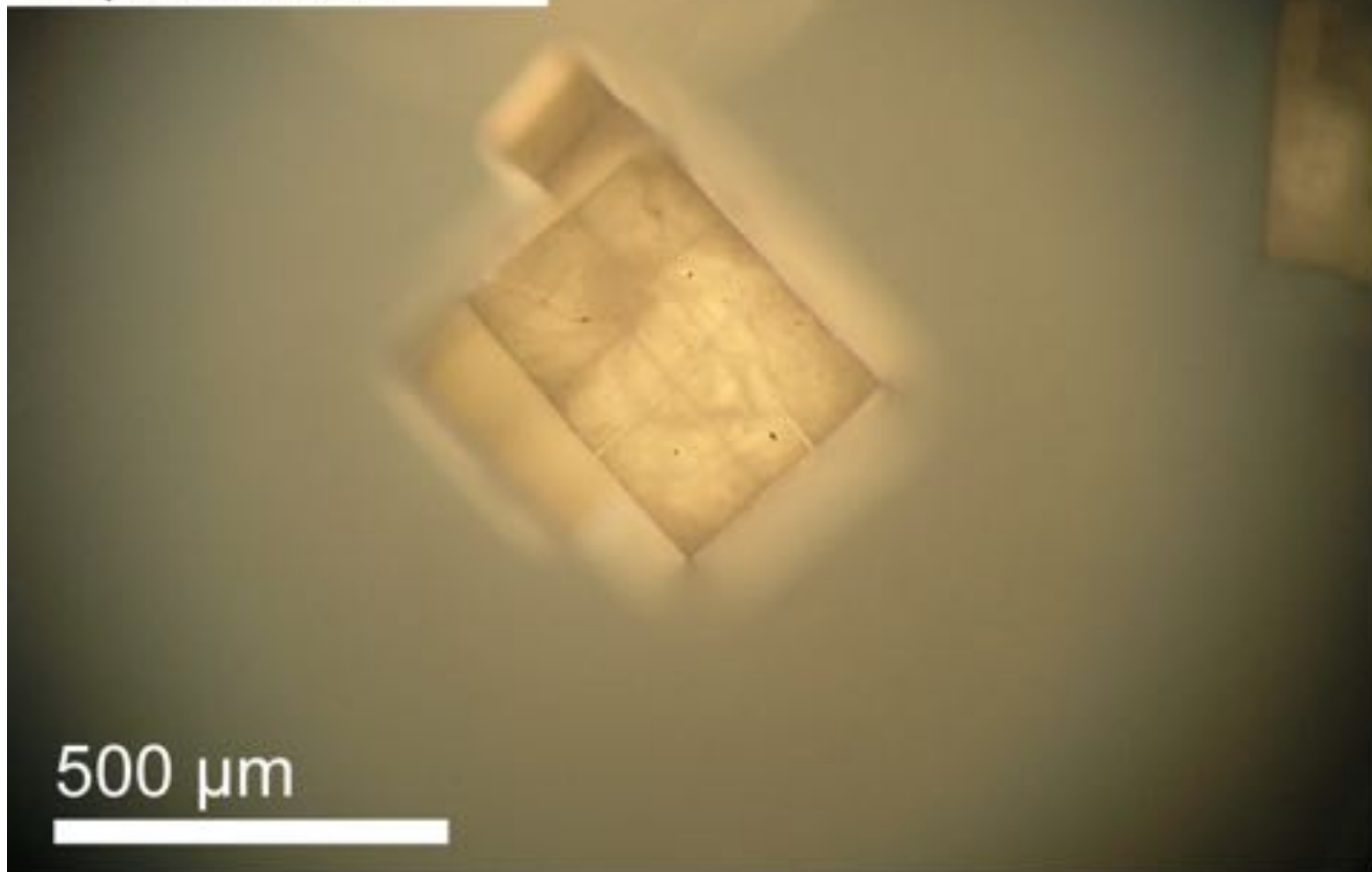
# Porous materials – Anomalous diffusion behavior



MOF5

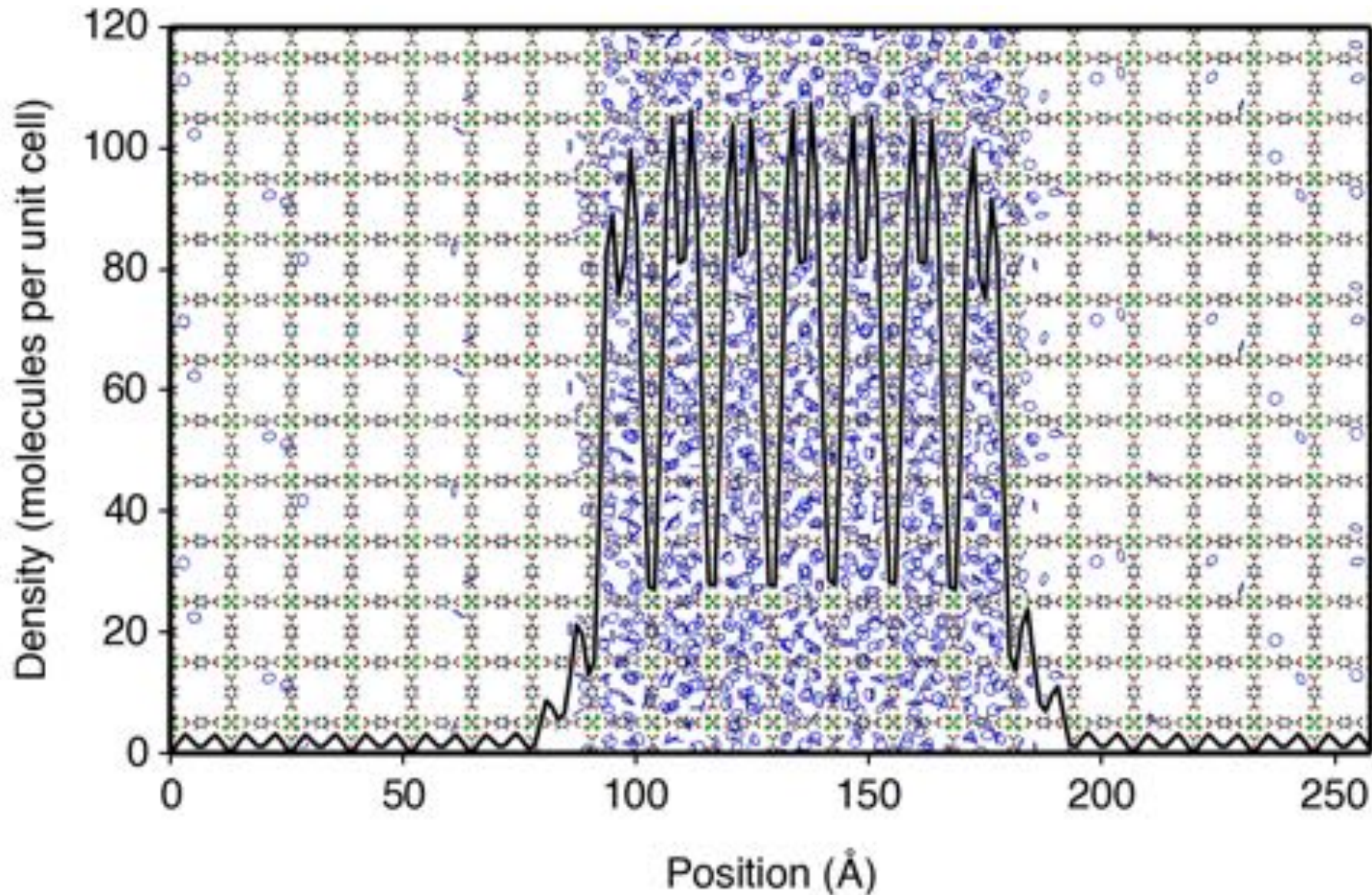
13:20:40 5-22-2014

Temperature: 25 C

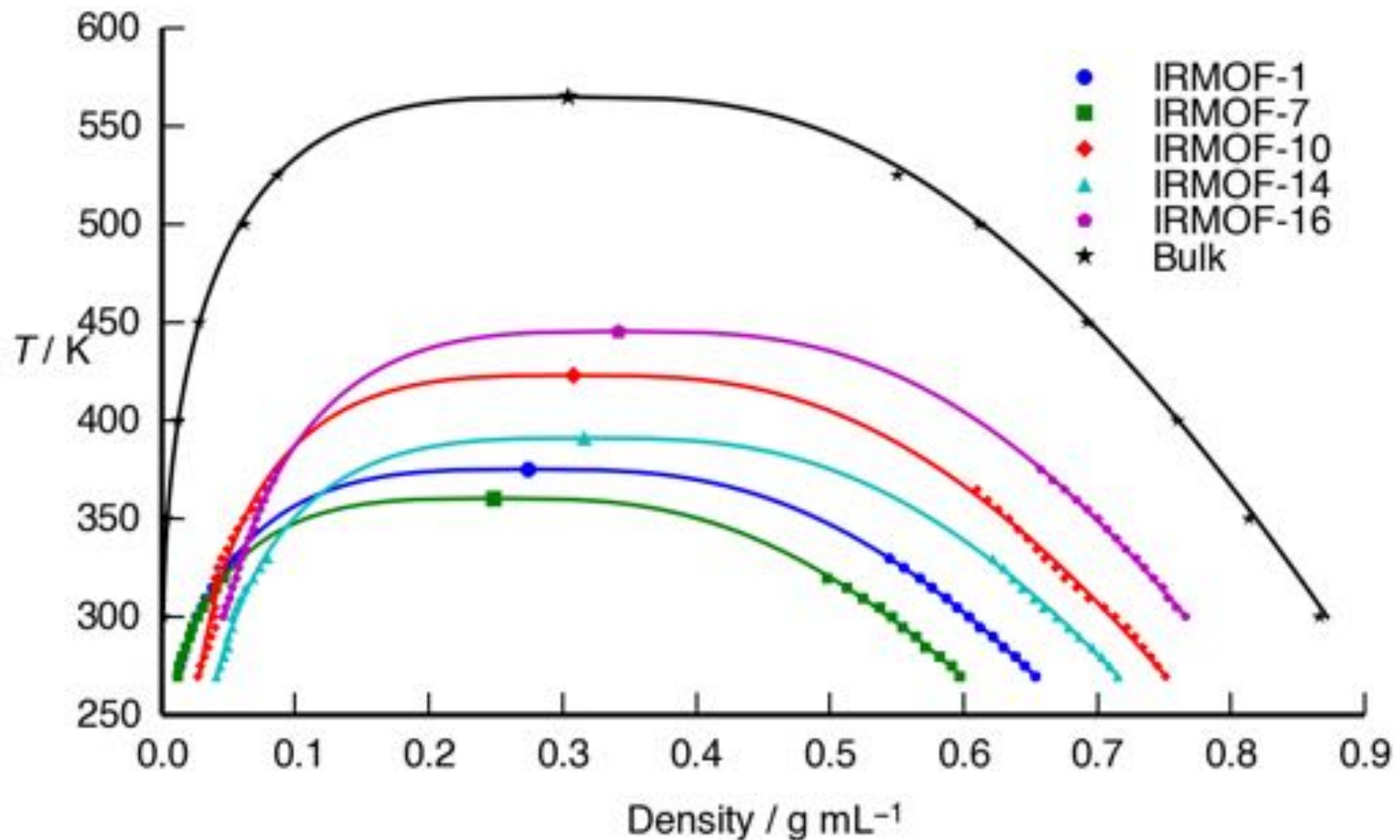




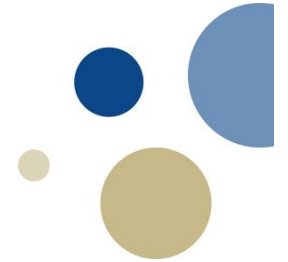
# Phase eq. in porous system



# Modifies critical point



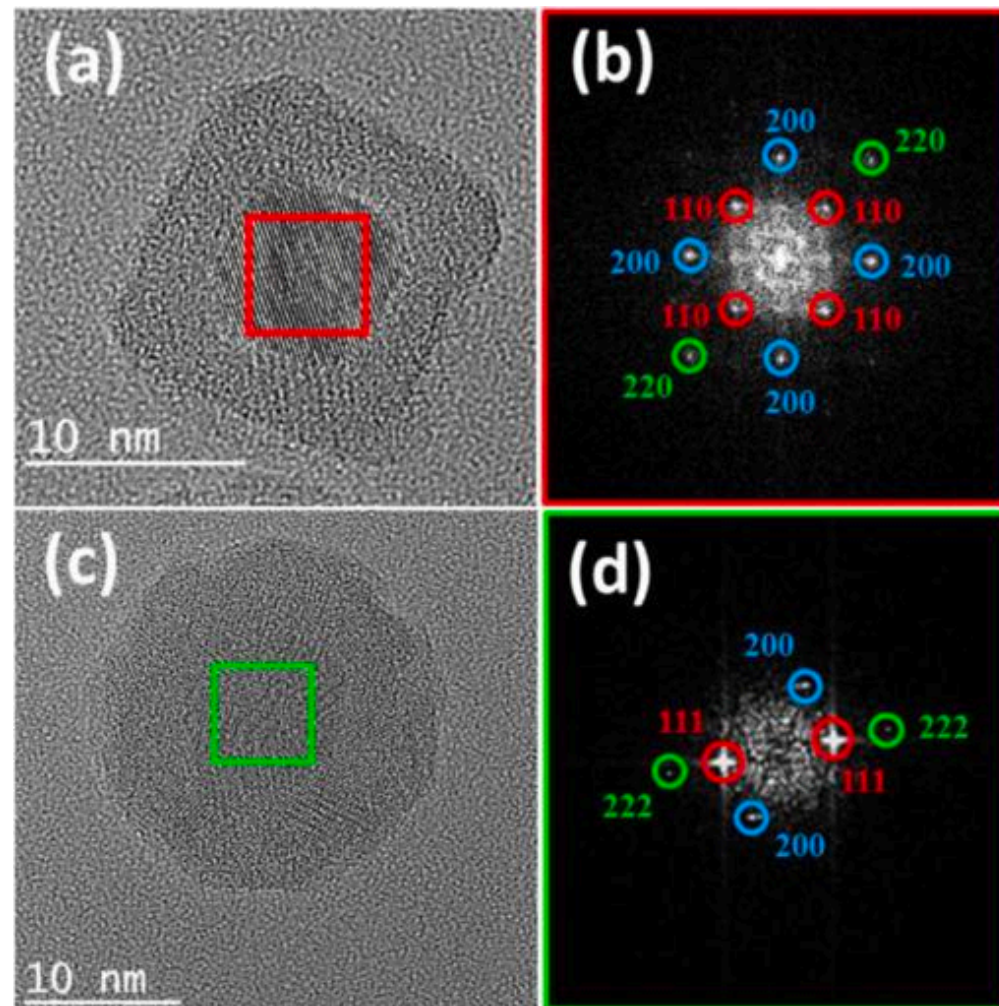
# Small droplets



- The equilibrium can be found in different materials
- Pore diameter smaller than what is expected to give capillary condensation
- Liquid phase extends beyond unitcell-diameter
  - but are still limited in size

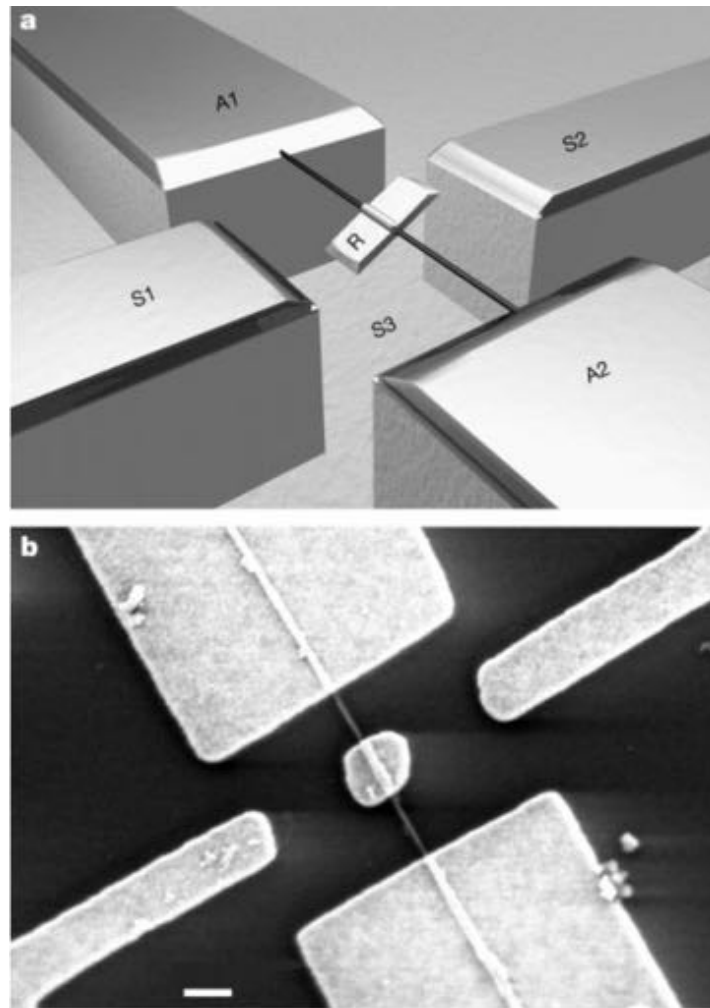


# Understanding nanoparticles





# Molecular machines



# Conclusion



- Thermodynamics still valid, even to very small systems
- Can calculate properties in bulk from sampling small systems
- True handle on KB integrals
- Not really clear how to use for actual small systems yet, need experimental collaborator

# Thanks to ...

- Signe Kjelstrup
- Dick Bedeaux
- Jean-Marc Simon
- Thijs J. H. Vlugt
- Bjørn Strøm
- Efrem Braun
- Berend Smit

